

**Dislocation Avalanches
from Strain Rate Controlled Loading:
A Discrete Dislocation Dynamics Study**

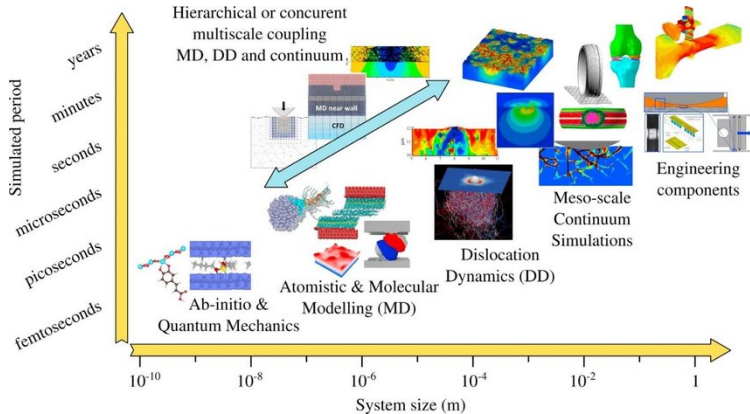
David Kurunczi-Papp and Lasse Laurson
david.kurunczi-papp@tuni.fi

"Interaction, Disorder, Elasticity"
workshop at Les Houches
April 3-7, 2023

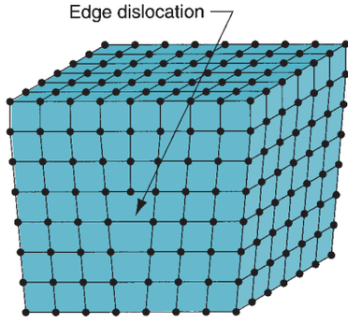
Plastic deformation



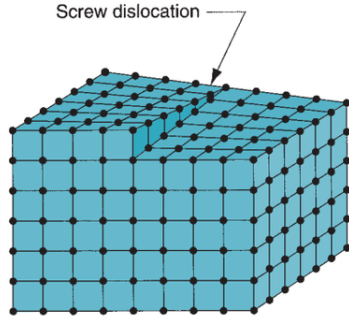
Scales



Dislocations

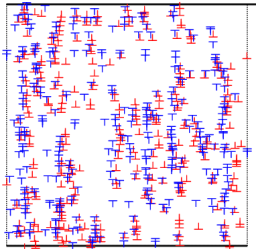


(a)

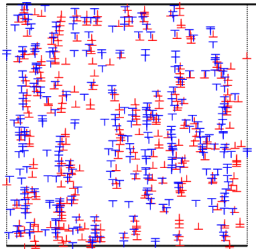


(b)

2D Discrete Dislocation Dynamics



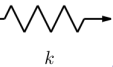
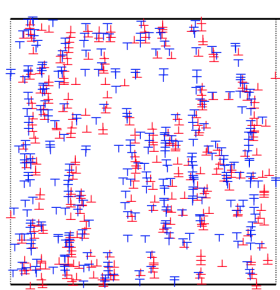
2D Discrete Dislocation Dynamics



$$\frac{\dot{x}_i}{Mb} = s_i b \left[\sum_{j \neq i} s_j \sigma_d(\mathbf{r}_i - \mathbf{r}_j) + \sigma \right],$$

$$\sigma_d(\mathbf{r}) = Db \frac{x(x^2 - y^2)}{(x^2 + y^2)^2}$$

Strain controlled loading

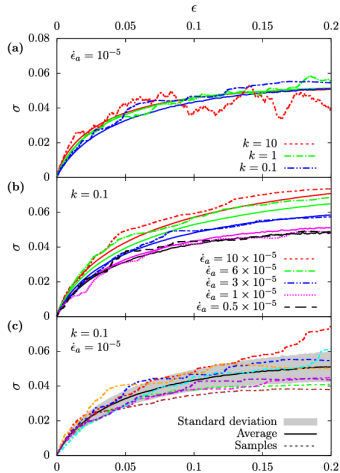


$$\frac{\dot{x}_i}{Mb} = s_i b \left[\sum_{j \neq i} s_j \sigma_d(\mathbf{r}_i - \mathbf{r}_j) + \sigma \right],$$

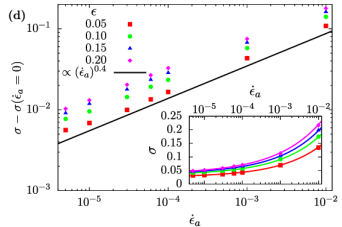
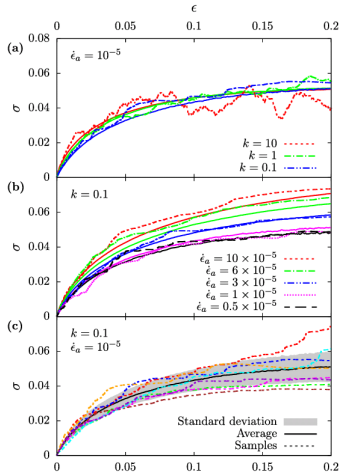
$$\sigma_d(\mathbf{r}) = Db \frac{x(x^2 - y^2)}{(x^2 + y^2)^2}$$

$$\sigma(t) = k [\dot{\epsilon}_a t - \epsilon(t)]$$

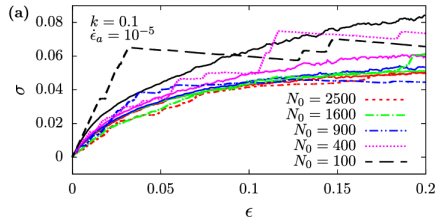
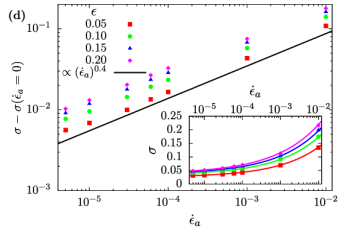
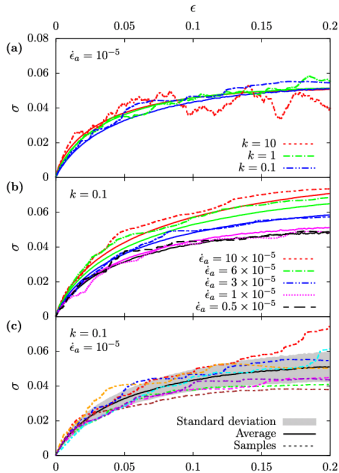
Stress-strain curves



Stress-strain curves

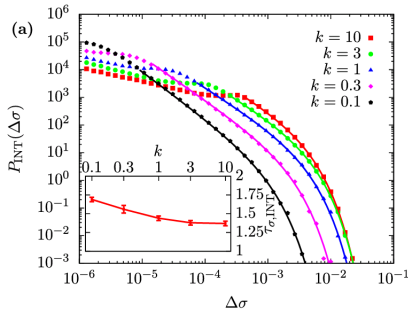


Stress-strain curves



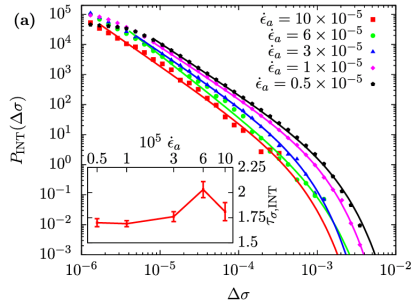
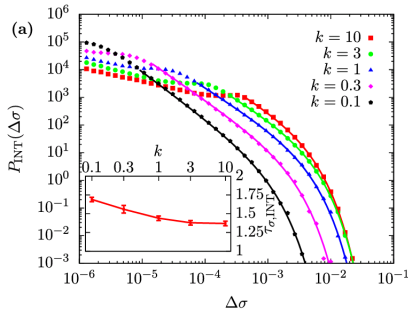
Stress drop magnitude distributions

$$P_{\text{INT}}(\Delta\sigma) \propto (\Delta\sigma)^{-\tau_\sigma} \exp\left(-\frac{\Delta\sigma}{\Delta\sigma_0}\right)$$



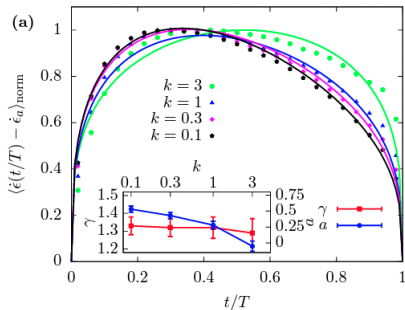
Stress drop magnitude distributions

$$P_{\text{INT}}(\Delta\sigma) \propto (\Delta\sigma)^{-\tau_\sigma} \exp\left(-\frac{\Delta\sigma}{\Delta\sigma_0}\right)$$



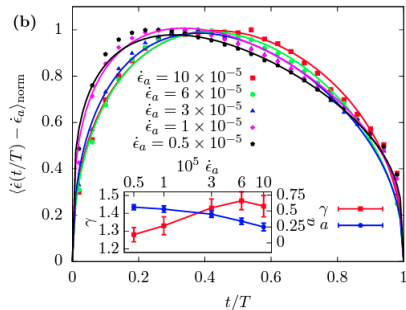
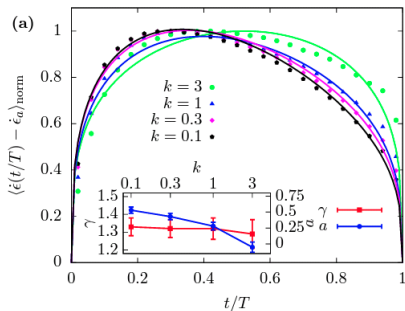
Average avalanche shapes

$$\langle \dot{\epsilon} \left(\frac{t}{T} \right) - \dot{\epsilon}_a \rangle \propto T^{\gamma-1} \left[\frac{t}{T} \left(1 - \frac{t}{T} \right) \right]^{\gamma-1} \left[1 - a \left(\frac{t}{T} - \frac{1}{2} \right) \right]$$



Average avalanche shapes

$$\langle \dot{\epsilon} \left(\frac{t}{T} \right) - \dot{\epsilon}_a \rangle \propto T^{\gamma-1} \left[\frac{t}{T} \left(1 - \frac{t}{T} \right) \right]^{\gamma-1} \left[1 - a \left(\frac{t}{T} - \frac{1}{2} \right) \right]$$



3D Discrete Dislocation Dynamics

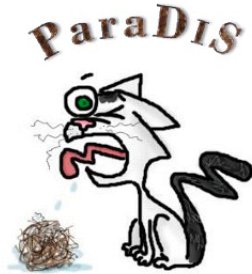
- ▶ Dislocation lines
- ▶ Mixed character
- ▶ Material specific mobility

3D Discrete Dislocation Dynamics

- ▶ Dislocation lines
- ▶ Mixed character
- ▶ Material specific mobility
- ▶ Complex system with complex dynamics

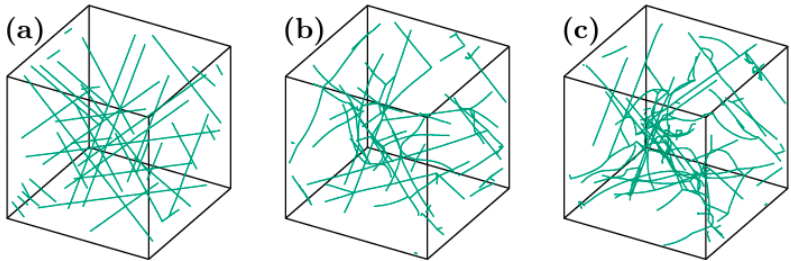
3D Discrete Dislocation Dynamics

- ▶ Dislocation lines
- ▶ Mixed character
- ▶ Material specific mobility
- ▶ Complex system with complex dynamics

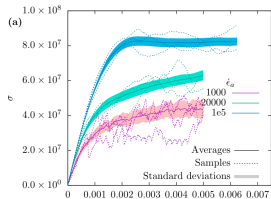


We create hairballs even a cat
wouldn't cough up

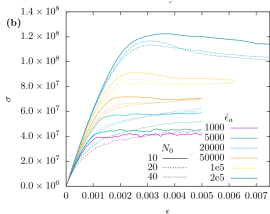
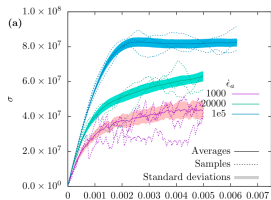
3D Discrete Dislocation Dynamics



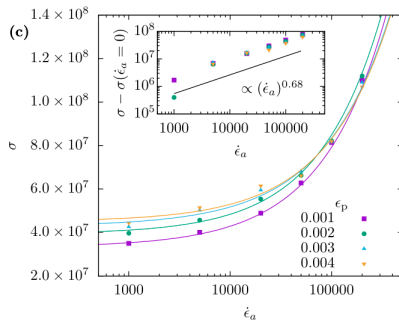
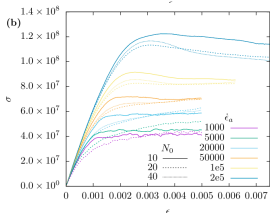
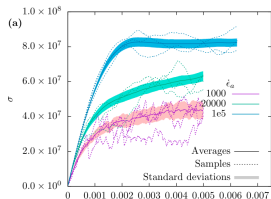
Stress-strain curves



Stress-strain curves

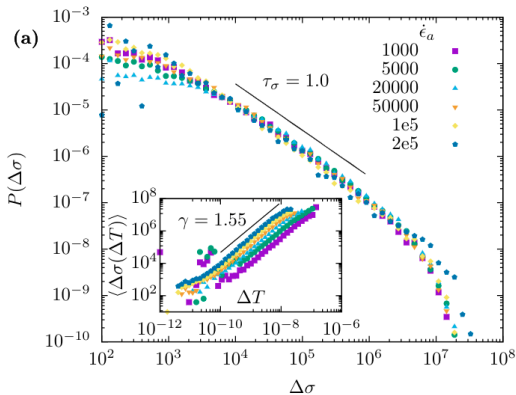


Stress-strain curves



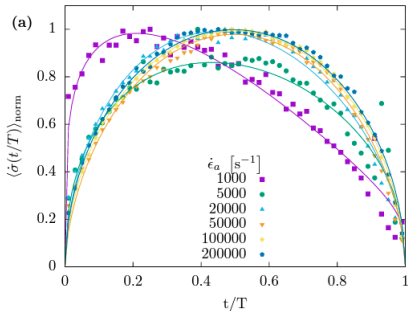
Stress drop magnitude distributions

$$P_{\text{INT}}(\Delta\sigma) \propto (\Delta\sigma)^{-\tau_\sigma} \exp\left(\frac{\Delta\sigma}{\Delta\sigma_0}\right)$$



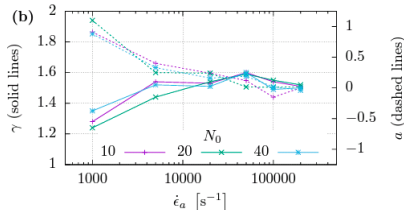
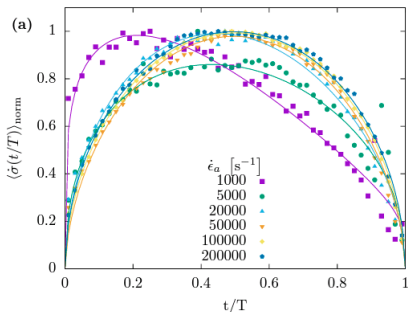
Average avalanche shapes

$$\langle \dot{\sigma} \left(\frac{t}{T} \right) \rangle \propto T^{\gamma-1} \left[\frac{t}{T} \left(1 - \frac{t}{T} \right) \right]^{\gamma-1} \left[1 - a \left(\frac{t}{T} - \frac{1}{2} \right) \right]$$

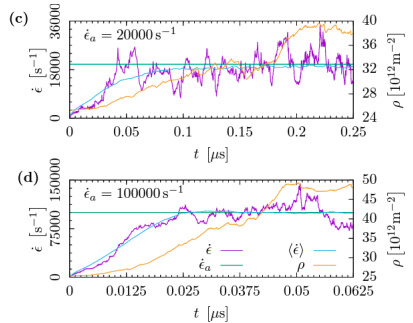
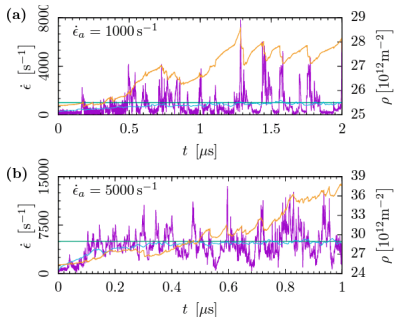


Average avalanche shapes

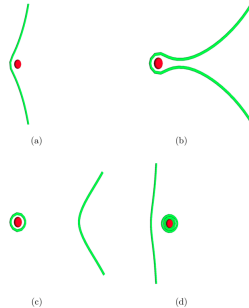
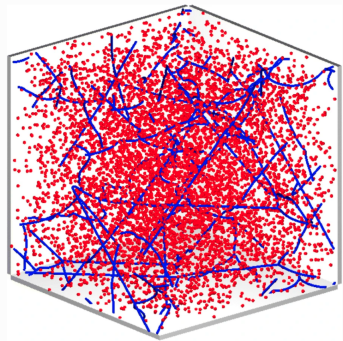
$$\langle \dot{\sigma} \left(\frac{t}{T} \right) \rangle \propto T^{\gamma-1} \left[\frac{t}{T} \left(1 - \frac{t}{T} \right) \right]^{\gamma-1} \left[1 - a \left(\frac{t}{T} - \frac{1}{2} \right) \right]$$



Asymmetry explained



Precipitates



Summary and conclusions

- ▶ Study the statistical properties of strain rate controlled loading of both 2D and 3D discrete dislocation simulations.
- ▶ Size- and rate dependence of the stress-strain curves
- ▶ In 2D the avalanche sizes are distributed by rate-dependent power laws, while in 3D the universal power law $\tau \approx 1.0$ is observed
- ▶ Rate dependent avalanche shapes with left asymmetries
- ▶ Several universality classes present in crystal plasticity

Thank you for Your attention!